

Algebra 2 GT Solving Quadratics Review

1st 3 Questions

- Solutions of quadratic equations represent the zeros (or x -intercepts) of a quadratic function.
- You can solve a quadratic equation by isolation, by completing the square, by using the quadratic formula, or by factoring.
- If a quadratic equation is not factorable, we can either complete the square or use the quadratic formula.

I. Isolation or Completing the Square

$$\begin{aligned} \text{I. } & \boxed{\text{II}} \quad x^2 - 8x - 5 = 0 \\ & x^2 - 8x + 16 = 5 + 16 \\ & (x-4)^2 = 21 \\ & x-4 = \pm\sqrt{21} \\ & x = 4 \pm \sqrt{21} \end{aligned}$$

$$\begin{aligned} \text{II. } & 5x^2 - 5 = 120 \\ & 5x^2 = 125 \\ & \boxed{x^2 = 25} \\ & \boxed{x = \pm 5} \end{aligned}$$

$$\begin{aligned} \text{III. } & 3x^2 + 9x + 9 = 3 \\ & x^2 + 3x + 3 = 1 \\ & x^2 + 3x = -2 \\ & x^2 + 3x + \frac{9}{4} = -2 + \frac{9}{4} \\ & \boxed{(x + \frac{3}{2})^2 = \frac{1}{4}} \end{aligned}$$

$$x + \frac{3}{2} = \pm \frac{1}{2}$$

$$\begin{aligned} & x = \frac{-3}{2} + \frac{1}{2} \\ & \boxed{x = -1} \end{aligned}$$

$$\begin{aligned} \text{IV. } & 6(x-2)^2 - 60 = 36 \\ & 6(x-2)^2 = 96 \\ & (x-2)^2 = 16 \\ & x-2 = \pm 4 \\ & x = 2 \pm 4 \\ & \boxed{x = 6, -2} \end{aligned}$$

$$5) 3(x+5)^2 + 32 = 64$$

$$3(x+5)^2 = 32$$

$$(x+5)^2 = \frac{32}{3}$$

$$x+5 = \pm \sqrt{\frac{32}{3}}$$

$$x+5 = \pm \frac{4\sqrt{3}}{\sqrt{3}} \left(\frac{\sqrt{3}}{\sqrt{3}}\right)$$

$$x+5 = \pm \frac{4\sqrt{6}}{3}$$

$$\boxed{x = -5 \pm \frac{4\sqrt{6}}{3}}$$

$$6) x^2 + 10x - 21 = 0$$

$$x^2 + 10x + 25 = 21 + 25$$

$$(x+5)^2 = 46$$

$$x+5 = \pm \sqrt{46}$$

$$\boxed{x = -5 \pm \sqrt{46}}$$

$$7) x^2 - 9x = 14x$$

$$x^2 - 14x + 49 = 9x + 49$$

$$(x-7)^2 = 144$$

$$x-7 = \pm \sqrt{144}$$

$$x-7 = \pm 12$$

$$x = 7 \pm 12$$

$$\boxed{x = 19, -5}$$

$$8) 2x^2 - 12x - 9 = 0$$
~~$$x^2 - 6x$$~~

$$2x^2 - 12x = 9$$

$$2(x^2 - 6x + 9) = 9$$

$$+ 18$$

$$2(x-3)^2 = 27$$

$$(x-3)^2 = \frac{27}{2}$$

$$(x-3) = \pm \sqrt{\frac{27}{2}} \cdot \frac{1}{2}$$

$$(x-3) = \pm \frac{3\sqrt{6}}{2}$$

$$\boxed{x = 3 \pm \frac{3\sqrt{6}}{2}}$$

II. Vertex Form

$$7) y = x^2 - 8x + 4$$

$$y = x^2 - 8x + 16 + 4 - 16$$

$$y = (x-4)^2 - 12$$

$$\boxed{y = (x-4)^2 - 12}$$

Vertex $(4, -12)$

8) $y = 2x^2 - 10x - 6$
 $y = 2(x^2 - 5x + \frac{25}{4}) - 6 - \frac{25}{2}$

$y = 2(x - \frac{5}{2})^2 - \frac{37}{2}$

Vertex $(\frac{5}{2}, -\frac{37}{2})$

9) $y = -3x^2 + 12x - 10$
 $-3(x^2 - 4x + 4) = 10 + 12$

$y = -3(x - 2)^2 + 2$

Vertex $(2, 2)$

III. Quadratic Formula

9. $2x^2 + 9x + 7 = 0$

$$x = \frac{-9 \pm \sqrt{(9)^2 - 4(2)(7)}}{2(2)}$$

$$x = \frac{-9 \pm \sqrt{81 - 56}}{4}$$

$$x = \frac{-9 \pm \sqrt{25}}{4}$$

$$x = \frac{-9 \pm 5}{4}$$

$x = -\frac{7}{2}, -1$

10) $2x^2 + 4x + 2 = 0$

$$x = \frac{-4 \pm \sqrt{(4)^2 - 4(2)(2)}}{2(2)}$$

$$x = \frac{-4 \pm \sqrt{0}}{4}$$

$x = -1$

$$11) 3+6x = -3x^2$$

$$\frac{3x^2 + 6x + 3}{3} = 0$$

$$x^2 + 2x + 1 = 0$$

$$x = \frac{-2 \pm \sqrt{(2)^2 - 4(1)(1)}}{2(1)}$$

$$x = \frac{-2 \pm \sqrt{0}}{2}$$

$$x = -1$$

$$12) x^2 + 3x - 5 = 0$$

$$x = \frac{-3 \pm \sqrt{(3)^2 - 4(1)(-5)}}{2(1)}$$

$$x = \frac{-3 \pm \sqrt{9 - 20}}{2}$$

$$x = \frac{-3 \pm \sqrt{-11}}{2}$$

No Real Solution!

$$13) x^2 + 6x - 25 = 0$$

$$x = \frac{-6 \pm \sqrt{(6)^2 - 4(1)(-25)}}{2(1)}$$

$$x = \frac{-6 \pm \sqrt{136}}{2}$$

$$x = \frac{-6 \pm 2\sqrt{34}}{2}$$

$$x = -3 \pm \sqrt{34}$$

$$14) x^2 - 14x = 5x$$

$$x^2 - 19x = 0$$

$$x = \frac{19 \pm \sqrt{(-19)^2 - 4(1)(0)}}{2(1)}$$

$$x = \frac{19 \pm \sqrt{361}}{2}$$

$$x = \frac{19 \pm 19}{2}$$

$$x = 19, 0$$

IV. Factoring

$$15) x^2 + 7x - 30 = 0$$

$$(x+10)(x-3) = 0$$

$$x = -10, 3$$

$$16) 3x^2 - 3x - 6 = 0$$

$$3(x^2 - x - 2) = 0$$

$$3(x-2)(x+1) = 0$$

$$x = 2, -1$$

$$17) x^2 - 81 = 0$$

$$(x+9)(x-9) = 0$$

$$x = -9, 9$$

$$18) x^2 + 6x - 40 = 0$$

$$(x+10)(x-4) = 0$$

$$x = -10, 4$$

$$19) 4x^2 - 25 = 0$$

$$(2x+5)(2x-5) = 0$$

$$x = -\frac{5}{2}, \frac{5}{2}$$

$$20) 2x^2 - 4x = 0$$

$$2x(x-2) = 0$$

$$x = 0, 2$$

$$21) 2x^2 + 13x + 15 = 0$$

$$(2x+3)(x+5) = 0$$

$$x = -\frac{3}{2}, -5$$

$$22) 3x^2 - 7x - 6 = 0$$

$$(3x+2)(x-3) = 0$$

$$x = -\frac{2}{3}, 3$$

$$23) 10x^2 - 17x + 3 = 0$$

$$(5x-1)(2x-3) = 0$$

$$x = \frac{1}{5}, \frac{3}{2}$$

$$24) 9x^2 - 4 = 0$$

$$(3x+2)(3x-2) = 0$$

$$x = -\frac{2}{3}, \frac{2}{3}$$

$$25) 3x^2 + 21x = 0$$

$$3x(x+7) = 0$$

$$x = 0, -7$$

$$26) x^2 - 3x - 54 = 0$$

$$(x-9)(x+6) = 0$$

$$x = 9, -6$$

IV Any Method

$$12) 3(x-5)^2 + 7 = 28$$

$$3(x-5)^2 = 21$$

$$(x-5)^2 = 7$$

$$x-5 = \pm\sqrt{7}$$

$$x = 5 \pm \sqrt{7}$$

$$13) 10 + 2(3x+2)^2 = 50$$

$$2(3x+2)^2 = 40$$

$$(3x+2)^2 = 20$$

$$3x+2 = \pm\sqrt{20}$$

$$x = \frac{-2 \pm 2\sqrt{5}}{3}$$

$$\begin{aligned} \boxed{14} \quad & x^2 - 3x + 4 = 10x - 38 \\ & x^2 - 13x + 42 = 0 \\ & (x-6)(x-7) = 0 \\ & \boxed{x=6, 7} \end{aligned}$$

$$\begin{aligned} \boxed{15} \quad & x^2 - 7x + 15 = 10 \\ & x^2 - 7x + 5 = 0 \\ & x = \frac{7 \pm \sqrt{(-7)^2 - 4(1)(5)}}{2(1)} \end{aligned}$$

$$\boxed{x = \frac{7 \pm \sqrt{29}}{2}}$$

$$\begin{aligned} \boxed{16} \quad & 8x^2 = 10x + 3 \\ & 8x^2 - 10x - 3 = 0 \\ & (4x - 3)(2x + 1) = 0 \\ & \boxed{x = \frac{3}{4}, -\frac{1}{2}} \end{aligned}$$

$$\begin{aligned} \boxed{17} \quad & -2x^2 + 5x + 4 = 0 \\ & x = \frac{-5 \pm \sqrt{(5)^2 - 4(-2)(4)}}{2(-2)} \end{aligned}$$

$$\boxed{x = \frac{-5 \pm \sqrt{57}}{-4}}$$

$$\boxed{x = \frac{5 \pm \sqrt{57}}{4}}$$

$$\begin{aligned} \boxed{18} \quad & x^2 - 12x + 35 = 0 \\ & (x-5)(x-7) = 0 \\ & \boxed{x = 5, 7} \end{aligned}$$

VI. Word Problems

$$\begin{aligned} \boxed{1} \quad & x = 1^{\text{st}} \text{ integer} \\ & x+1 = 2^{\text{nd}} \text{ integer} \end{aligned}$$

$$\begin{aligned} & x(x+1) = 240 \\ & x^2 + x - 240 = 0 \\ & (x+16)(x-15) = 0 \\ & \boxed{x = -16, 15} \end{aligned}$$

The consecutive integers are either -16 & -15 or $15, 16$.

26) $h(t) = -4.9t^2 + 10$

a) $-4.9t^2 + 10 = 0$

$$-4.9t^2 = -10$$

$$\Rightarrow t^2 = \frac{10}{4.9}$$

$$t = \pm \sqrt{\frac{10}{4.9}}$$

$$t \approx 1.43 \text{ seconds}$$

In about 1.43 seconds, the hammer will hit the ground.

b) $h(0.5) = -4.9(0.5)^2 + 10 = 8.775$

After .5 seconds, the hammer is at about 8.775 meters.

c) $-4.9t^2 + 10 = 5$

$$-4.9t^2 = -5$$

$$t^2 = \frac{5}{4.9}$$

$$t = \pm \sqrt{\frac{5}{4.9}}$$

$$t \approx 1.01$$

The hammer will be 5 ft of the ground at about 1.01 seconds after it was dropped.

d) $h(t) = -4.9t^2 + 10$

Vertex $(0, 10)$

At the time the hammer is dropped ($t=0$), it is at a height of 10 meters.

30) $h(t) = -4.9t^2 + 19.6t$

a) $-4.9t^2 + 19.6t = 0$
 $-4.9t(t - 4) = 0$
 $t = 0 \quad t = 4$

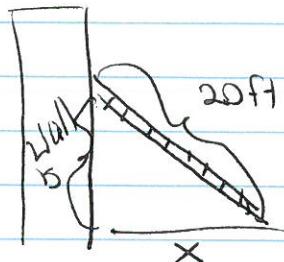
The ball is in the air for 4 seconds.

b) $h = -4.9(t^2 - 4t)$
 $h = -4.9(t^2 - 4t + 4) + 4.9(4)$

$h = -4.9(t - 2)^2 + 19.6$

The maximum height of the ball is 19.6 meters.

29)



$$\begin{aligned} x^2 + 15^2 &= 20^2 \\ x^2 + 225 &= 400 \\ x^2 &= 175 \end{aligned}$$

$x = 13.23 \text{ ft}$